

Online-and-Offline Partial Evaluation: A Mixed Approach

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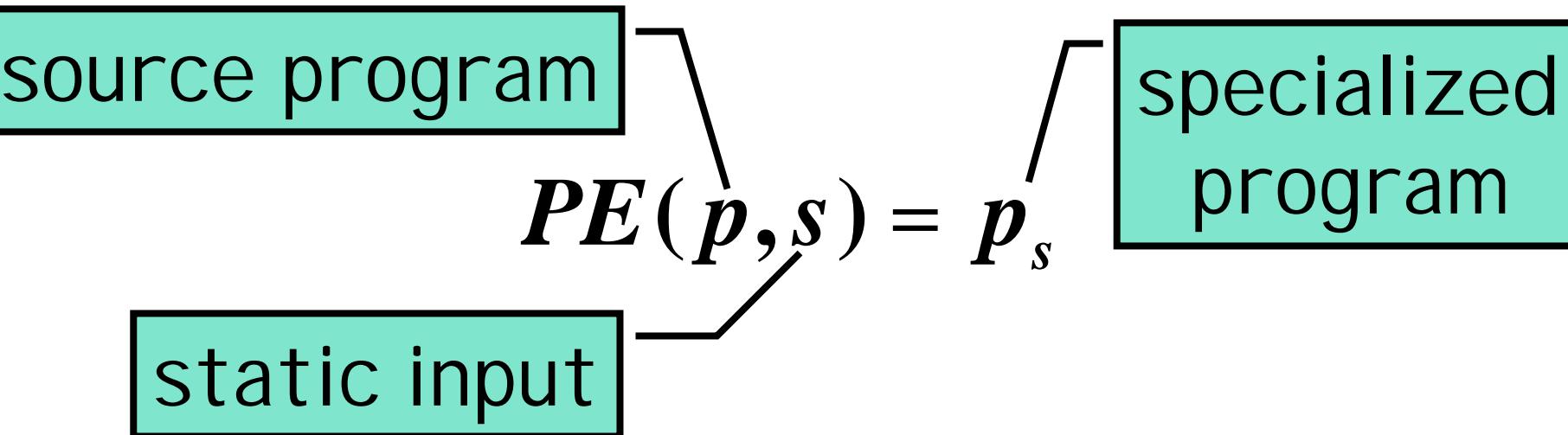
Overview

- Introduction
- Simple Online PE
- Our Method
- Experiments
- Related Work
- Conclusion

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Partial Evaluation



- *Reduce static computations*
- *Residualize dynamic computations*

s.t. $p_s(d) = p(s, d)$ for any d

dynamic input

Two Issues in PE

1. Efficiency of *specialized programs*

(analogy: efficiency of compiled programs)

2. Efficiency of *specialization*

(analogy: efficiency of compilation)

Both are important.

Online PE and Offline PE

When to decide whether a computation is static or dynamic?

- Online PE:

During the specialization,
with a static input

- Offline PE:

Before the specialization,
w/o a static input

Online v.s. Offline

Online PE (analogy: dynamic typing)

- Finer decision
 - ⇒ faster *specialized programs*

Offline PE (analogy: static typing)

- Faster *specialization*
- Easier reasoning

Either approach has its advantage.

Our Approach

Hybrid of online/offline PE
(analogy: soft typing)

- Make an offline decision so far as it is precise
- Otherwise, make an online decision

Results

- Specialized programs:
as fast as simple online PE
- Specialization:
1.5-8 times faster than
simple offline PE
(for the same specialization)
 - thanks to the decrease of
unnecessary let-insertions
(explained later)

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Symbolic Values

dynamic expression
for residualization

`type a symval = a option ` exp`

static value
for reduction
(optional)

`type a option = Some a | None`

Simple Online PE

$$[| x |] = x$$

$$[| \lambda x.e |] = \text{á}Some(\textcolor{blue}{\lambda x.[| e |]}), \underline{\lambda x'} \dots \tilde{n}$$

$$[| e_1 e_2 |] = \text{case } [| e_1 |]$$

of $\text{á}Some \ s, \ \tilde{n} \models s [| e_2 |]$

| $\text{á}None, \ d \models \text{á}None, \ d \ \underline{@} \ \text{snd } [| e_2 |]$ \tilde{n}

Let-Insertion is Necessary

- to preserve semantics under effects
- to avoid code duplication

Let-Insertion is Necessary

- to preserve semantics under effects

$\lfloor f. \text{let } y = fx \text{ in } 1+2 \rfloor$

→ $\lfloor f. \text{let } y = fx \text{ in } 3 \rfloor$

rather than $\lfloor f. 3 \rfloor$

- to avoid code duplication

Let-Insertion is Necessary

- to preserve semantics under effects
- to avoid code duplication

let $f = \lambda x.1+2$ in (f,f)

→ **let $f = \lambda x.3$ in (f,f)**

rather than **$(\lambda x.3, \lambda x.3)$**

Simple Online PE

$$[| x |] = x$$

$$[| \lambda x.e |] = \text{á}Some(\lambda x.[| e |]), \underline{\lambda x'} \dots \tilde{n}$$

$$[| e_1 e_2 |] = \text{case } [| e_1 |]$$

of á*Some s, _* ñ P *s [| e_2 |]*

| á*None, d* ñ P á*None, d @ snd [| e_2 |]*ñ

Simple Online PE with Let-Insertion

$$[| x |] = x$$

$$[| \lambda x.e |] = \text{á}Some(\lambda x.delimit-let([| e |])), \\ \textcolor{magenta}{insert-let}(\underline{\lambda x'}....) \tilde{n}$$

$$[| e_1 e_2 |] = \text{case } [| e_1 |] \\ \text{of á}Some\ s, \ \tilde{n}\ \text{P } s\ [| e_2 |]$$

$$\quad | \text{á}None, d \tilde{n} \text{P} \\ \text{á}None, \textcolor{magenta}{insert-let}(d \underline{@} \text{snd } [| e_2 |]) \tilde{n}$$

Simple Online PE is Slow

because of:

- unnecessary tagging (*None/Some*)
- unnecessary let-insertion
- unnecessary residualization

$[] (\lambda x.x)3 [] =$

case $\text{á} \textcolor{magenta}{Some}(\lambda x.x)$, *insert-let*($\lambda x'$...)ñ

of $\text{á} \textcolor{magenta}{Some}(s)$, _ñ $\vdash s 3$

| $\text{á} \textcolor{magenta}{None}$, dñ $\vdash ...$

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of $\text{á} \textcolor{magenta}{Some}(s)$, $_ \tilde{n} \vdash s 3$

| $\text{á} \textcolor{magenta}{None}$, $d \tilde{n} \vdash \dots$

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$[] (\lambda x.x)3 [] =$

case $\lambda \underline{x}.\underline{x}$, *let-insert*($\underline{\lambda x' \dots}$) \tilde{n}

of $\tilde{as}, \underline{\tilde{n}} \vdash s 3$

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because of:

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$[] (\lambda x.x)3 [] =$

case $\lambda x.x$, *let-insert*($\lambda x'$...)ñ

of $\lambda s, __ P\ s\ 3$

Simple Online PE is Slow

because of:

- unnecessary tagging (*None/Some*)
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- unnecessary residualization

$\lambda x.x \ 3 =$
case $\lambda x.x$
of $s \vdash s \ 3$

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What Information is Useful?

- A static value is...
 - always/never available
⇒ Tagging becomes unnecessary
- A dynamic expression...
 - never remains
⇒ Residualization becomes unnecessary
 - remains at most once (& has no effects)
⇒ Let-insertion becomes unnecessary

Types

r (raw type) ::= b_i | $t_1 \rightarrow t_2$ | $t_1 \times t_2$

t (annotated type) ::= $r^{(s,d)}$

s (static use) ::= **0** (never) | **w** (always)
| **T** (sometimes)

"Whether a static value is available"

d (dynamic use) ::= **0** (never)
| **1** (at most once) | **w** (any number of times)

*"How many times
a dynamic expression remains"*

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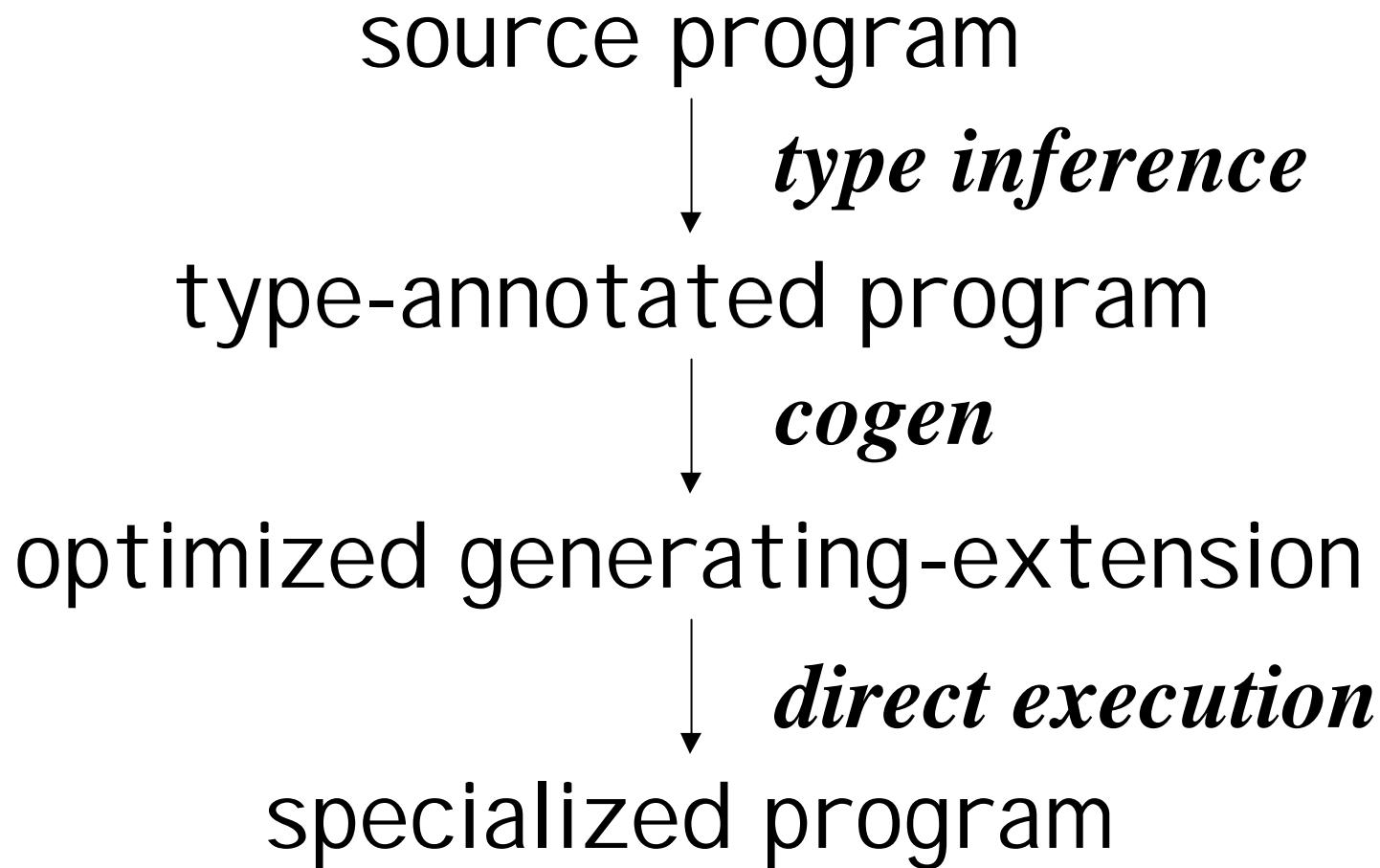
"Whether a static value is available"

d (dynamic use) ::= 0 (never)

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*"How many times
a dynamic expression remains"*

Framework of our Method



Examples of Typing (I): Static Uses (0, w, and T)

$\lambda g. \text{let } f : \text{int}^R(0,1) \text{ } a = g \text{ in } f\ 3$

→ $\underline{\lambda g. \text{let } f = g \text{ in }} \underline{f @ 3}$

→ $\underline{\lambda g. g @ 3}$

$\lambda g. \text{let } f : \text{int}^R(w,0) \text{int} = \lambda x.x \text{ in } f\ 3$

→ $\underline{\lambda g. \text{let } f = \lambda x.x \text{ in }} \underline{f @ 3}$

→ $\underline{\lambda g. 3}$

$\lambda g. \text{let } f : \text{int}^R(T,1) \text{int} = (\text{if } true \text{ then } \lambda x.x \text{ else } g)$
in f 3

→ $\underline{\lambda g. \text{let } f = (\text{if } true \text{ then } \text{á}Some(\lambda x.x), \frac{1}{4})}$

Examples of Typing (I): Static Uses (0, w, and T)

```
l g. let f = g in f 3
```

Examples of Typing (I): Static Uses (0, w, and T)

```
l g. let f : int®(0,1) a = g in f 3
```

Examples of Typing (I): Static Uses (0, w, and T)

l g. let $f : \text{int}^{\textcircled{R}}(0,1)$ $a = g$ in $f\ 3$

⇒ l g. let $f = g$ in $f@3$

Examples of Typing (I): Static Uses (0, w, and T)

l g. let $f : \text{int}^{\text{R}}(0,1)$ $a = g$ in $f\ 3$

→ l g. let $f = g$ in $f@3$

→ l g. g@3

Examples of Typing (I): Static Uses (0, w, and T)

l g. let $f : \text{int} \circledR^{(0,1)} a = g$ in $f\ 3$

→ l g. let $f = g$ in $f@3$

→ l g. g@3

l g. let $f = \mathbf{l}\ x.\ x$ in $f\ 3$

Examples of Typing (I): Static Uses (0, w, and T)

$\lambda g. \text{let } f : \text{int} @^{(0,1)} a = g \text{ in } f 3$

→ $\underline{\lambda g. \text{let } f = g \text{ in } f @ 3}$

→ $\underline{\lambda g. g @ 3}$

$\lambda g. \text{let } f : \text{int} @^{(w,0)} \text{int} = \lambda x. x \text{ in } f 3$

Examples of Typing (I): Static Uses (0, w, and T)

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Examples of Typing (I): Static Uses (0, w, and T)

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→ $\underline{\lambda g. 3}$

Examples of Typing (I): Static Uses (0, w, and T)

$\text{lg. let } f : \text{int}^{\mathbb{R}(0,1)} a = g \text{ in } f 3 \Rightarrow \text{lg. } g 3$

$\text{lg. let } f : \text{int}^{\mathbb{R}(w,0)} \text{int} = \lambda x.x \text{ in } f 3 \Rightarrow \text{lg. } 3$

$\text{lg. let } f = (\text{if } true \text{ then } \lambda x.x \text{ else } g)$
in f 3

Examples of Typing (I): Static Uses (0, w, and T)

$\text{lg. let } f : \text{int}^R(0,1) a = g \text{ in } f 3 \Rightarrow \text{lg. } g 3$

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$\text{lg. let } f : \text{int}^R(T,1) \text{int} = (\text{if } true \text{ then } \lambda x.x \text{ else } g)$
in f 3

Examples of Typing (I): Static Uses (0, w, and T)

$\lg. \text{let } f : \text{int} @^{(0,1)} a = g \text{ in } f 3 \rightarrow \lg. g 3$

$\lg. \text{let } f : \text{int} @^{(w,0)} \text{int} = \lambda x.x \text{ in } f 3 \rightarrow \lg. 3$

$\lg. \text{let } f : \text{int} @^{(T,1)} \text{int} = (\text{if } true \text{ then } \lambda x.x \text{ else } g)$
 $\text{in } f 3$

$\Rightarrow \underline{\lg. \text{let } f = (\text{if } true \text{ then } \text{á}Some(\lambda x.x), \frac{1}{4})}$

$\text{else á}None, g\tilde{n})$

$\text{in } (\text{case } f \text{ of } \text{á}Some s, _\tilde{n} \vdash s 3$

$| \text{á}None, d\tilde{n} \vdash d@3)$

Examples of Typing (I): Static Uses (0, w, and T)

$\lg. \text{let } f : \text{int} @^{(0,1)} a = g \text{ in } f 3 \rightarrow \lg. g 3$

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$| \text{á}None, d\tilde{n} \vdash d@3)$

$\rightarrow \underline{\lg. 3}$

Examples of Typing (II): Dynamic Uses (0, 1, and w)

$\text{let } f : \text{int}^{\text{R}(0,0)} \text{int} = \lambda x. 1+2+x \text{ in } 7$

→ $\text{let } f = \lambda \text{ in } 7$

→ 7

$\text{let } f : \text{int}^{\text{R}(0,1)} \text{int} = \lambda x. 1+2+x \text{ in } f$

→ $\text{let } f = \underline{\lambda x. 1+2+x} \text{ in } f$

→ $\underline{\lambda x. 3+x}$

$\text{let } f : \text{int}^{\text{R}(0,w)} \text{int} = \lambda x. 1+2+x \text{ in } \tilde{f}, f$

→ $\text{let } f = \text{insert-let}(\lambda x. 1+2+x) \text{ in } (f, f)$

→ $\text{let } f' = \underline{\lambda x. 3+x} \text{ in } (f', f)$

Examples of Typing (II): Dynamic Uses (0, 1, and w)

```
let f = λx.1+2+x in 7
```

Examples of Typing (II): Dynamic Uses (0, 1, and w)

```
let f : int®(0,0)int = λx.1+2+x in 7
```

Examples of Typing (II): Dynamic Uses (0, 1, and w)

let f : int $\mathbb{R}^{(0,0)}$ int = $\lambda x.1+2+x$ in 7

⇒ let f = λ in 7

Examples of Typing (II): Dynamic Uses (0, 1, and w)

let f : int $\mathbb{R}^{(0,0)}$ int = $\lambda x.1+2+x$ in 7

⇒ let f = λ in 7

⇒ 7

Examples of Typing (II): Dynamic Uses (0, 1, and w)

let f : int $\mathbb{R}^{(0,0)}$ int = $\lambda x.1+2+x$ in 7

→ let f = $\lambda x.1+2+x$ in 7

→ 7

let f = $\lambda x.1+2+x$ in f

Examples of Typing (II): Dynamic Uses (0, 1, and w)

let f : int $\mathbb{R}^{(0,0)}$ int = $\lambda x.1+2+x$ in 7

→ let f = $\lambda x.1+2+x$ in 7

→ 7

let f : int $\mathbb{R}^{(0,1)}$ int = $\lambda x.1+2+x$ in f

Examples of Typing (II): Dynamic Uses (0, 1, and w)

let f : int $\mathbb{R}^{(0,0)}$ int = $\lambda x.1+2+x$ in 7

⇒ let f = $\lambda x.1+2+x$ in 7

⇒ 7

let f : int $\mathbb{R}^{(0,1)}$ int = $\lambda x.1+2+x$ in f

⇒ let f = $\lambda x.1+2+x$ in f

Examples of Typing (II): Dynamic Uses (0, 1, and w)

`let f : intR(0,0)int = l x.1+2+x in 7`

→ `let f = _ in 7`

→ `7`

`let f : intR(0,1)int = l x.1+2+x in f`

→ `let f = l x.1+2+x in f`

→ `l x.3+x`

Examples of Typing (II): Dynamic Uses (0, 1, and w)

let f : int $\mathbb{R}^{(0,0)}$ int = $\lambda x.1+2+x$ in 7

→ let f = $\lambda x.1+2+x$ in 7

→ 7

let f : int $\mathbb{R}^{(0,1)}$ int = $\lambda x.1+2+x$ in f

→ let f = $\lambda x.1+2+x$ in f

→ $\lambda x.3+x$

let f = $\lambda x.1+2+x$ in $\tilde{f}, f\tilde{n}$

Examples of Typing (II): Dynamic Uses (0, 1, and w)

let f : int $\mathbb{R}^{(0,0)}$ int = $\lambda x.1+2+x$ in 7

→ let f = λ in 7

→ 7

let f : int $\mathbb{R}^{(0,1)}$ int = $\lambda x.1+2+x$ in f

→ let f = $\lambda x.1+2+x$ in f

→ $\lambda x.3+x$

let f : int $\mathbb{R}^{(0,w)}$ int = $\lambda x.1+2+x$ in $\tilde{f}, f\tilde{n}$

Examples of Typing (II): Dynamic Uses (0, 1, and w)

$\text{let } f : \text{int}^{\mathbb{R}(0,0)} \text{int} = \lambda x. 1+2+x \text{ in } 7$

⇒ $\text{let } f = \lambda \text{ in } 7$

⇒ 7

$\text{let } f : \text{int}^{\mathbb{R}(0,1)} \text{int} = \lambda x. 1+2+x \text{ in } f$

⇒ $\text{let } f = \underline{\lambda x. 1+2+x} \text{ in } f$

⇒ $\underline{\lambda x. 3+x}$

$\text{let } f : \text{int}^{\mathbb{R}(0,w)} \text{int} = \lambda x. 1+2+x \text{ in } \tilde{f}, f$

⇒ $\text{let } f = \textcolor{magenta}{\text{insert-let}}(\underline{\lambda x. 1+2+x}) \text{ in } (\tilde{f}, f)$

Examples of Typing (II): Dynamic Uses (0, 1, and w)

$\text{let } f : \text{int} @^{(0,0)} \text{int} = \lambda x. 1 + 2 + x \text{ in } 7$

→ $\text{let } f = \underline{\hspace{2cm}} \text{ in } 7$

→ $\underline{\hspace{2cm}}$

$\text{let } f : \text{int} @^{(0,1)} \text{int} = \lambda x. 1 + 2 + x \text{ in } f$

→ $\text{let } f = \underline{\lambda x. 1 + 2 + x} \text{ in } f$

→ $\underline{\lambda x. 3 + x}$

$\text{let } f : \text{int} @^{(0,w)} \text{int} = \lambda x. 1 + 2 + x \text{ in } \tilde{f}, f$

→ $\text{let } f = \textcolor{magenta}{\text{insert-let}}(\lambda x. 1 + 2 + x) \text{ in } (\tilde{f}, f)$

→ $\text{let } f = \underline{\lambda x. 3 + x} \text{ in } (\tilde{f}, f)$

Example of Typing Rules

For λ -abstractions:

$$G \succ (s, d) \times G_0$$

$$d^{-1} 0 \vdash s_1^{-1} W$$

$$\frac{G_0, x : r_1^{(s_1, d_1)} \quad e : t_2}{G \quad \lambda x. e : r_1^{(s_1, d_1)} \circledR^{(s, d)} t_2} (\text{abs})$$

Type Inference

- Construct a type derivation
 - assign use variables
 - generate constraints on them
- Solve the constraints

Type Inference

- Construct a type derivation
- Solve the constraints
 - approximate most conservatively
(every $s = T$ and every $d = w$)
 - refine by iterations
 $(\mathbf{0} \prec_S w \prec_S T \text{ and } \mathbf{0} \prec_D 1 \prec_D w)$
 - linear w.r.t. the # of use variables
 - can be stopped at any time

Type Inference

- Construct a type derivation
- Solve the constraints
 - approximate most conservatively
(every $s = \mathbf{T}$ and every $d = w$)
 - refine by iterations
 $(\mathbf{0} \prec_S w \prec_S \mathbf{T} \text{ and } \mathbf{0} \prec_D 1 \prec_D w)$

N.B. The existence of \mathbf{T}
simplified the analysis with 1

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Compared Methods

- Simple Online PE: only (T,w) with post-processing for inlining
- Simple Offline PE: $(w,0)$ and $(0,w)$ with binding-time improvement *by hand*
- [Sperber-96]: $(w,0)$, $(0,w)$, and (T,w)
- Our Method

All are implemented with:

- a cogen approach
- state-based let-insertion

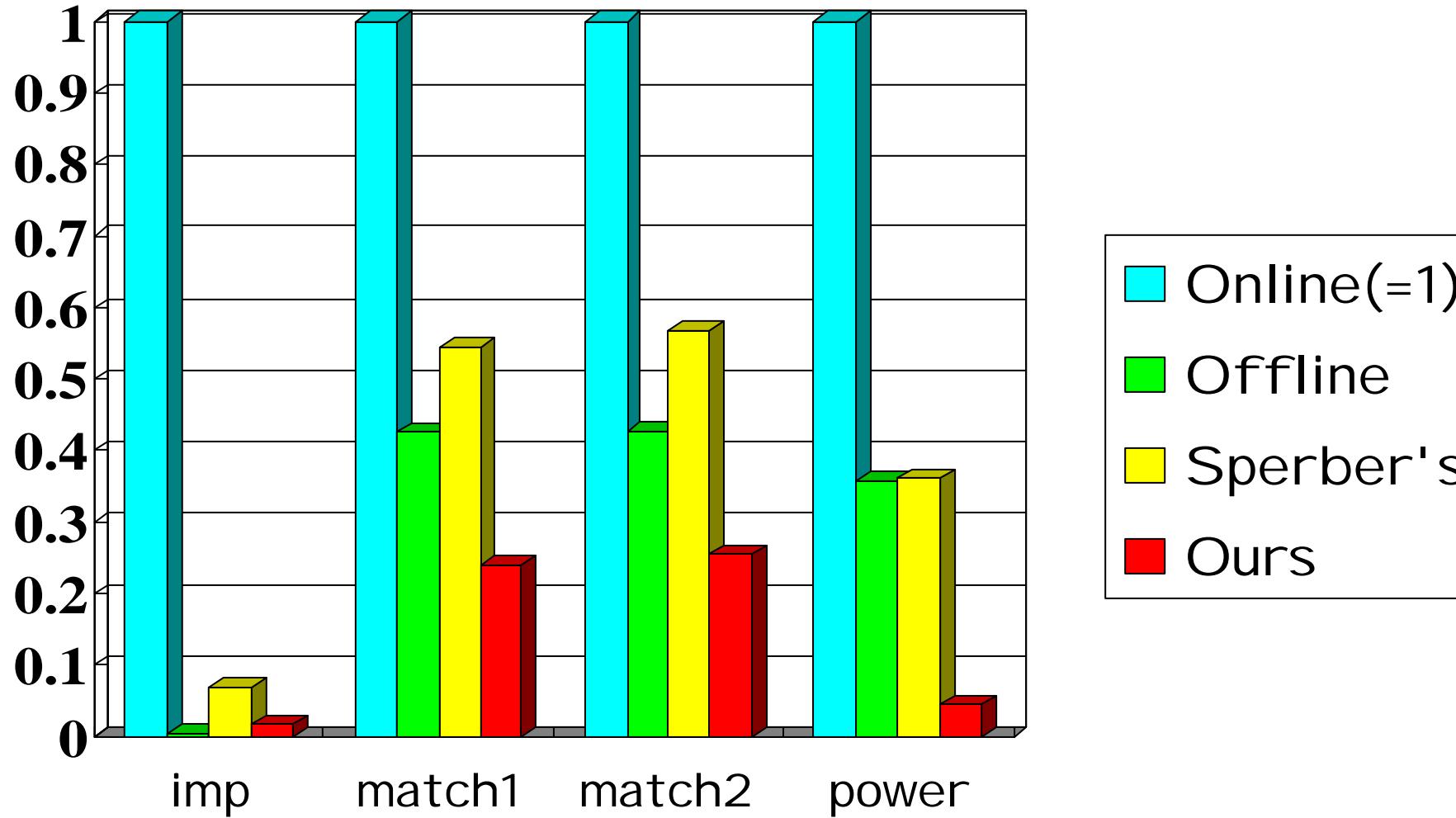
Applications

- imp: an interpreter for a simple imperative language
- match1: a pattern matcher with the pattern static
- match2: the same pattern matcher with the string static
- power

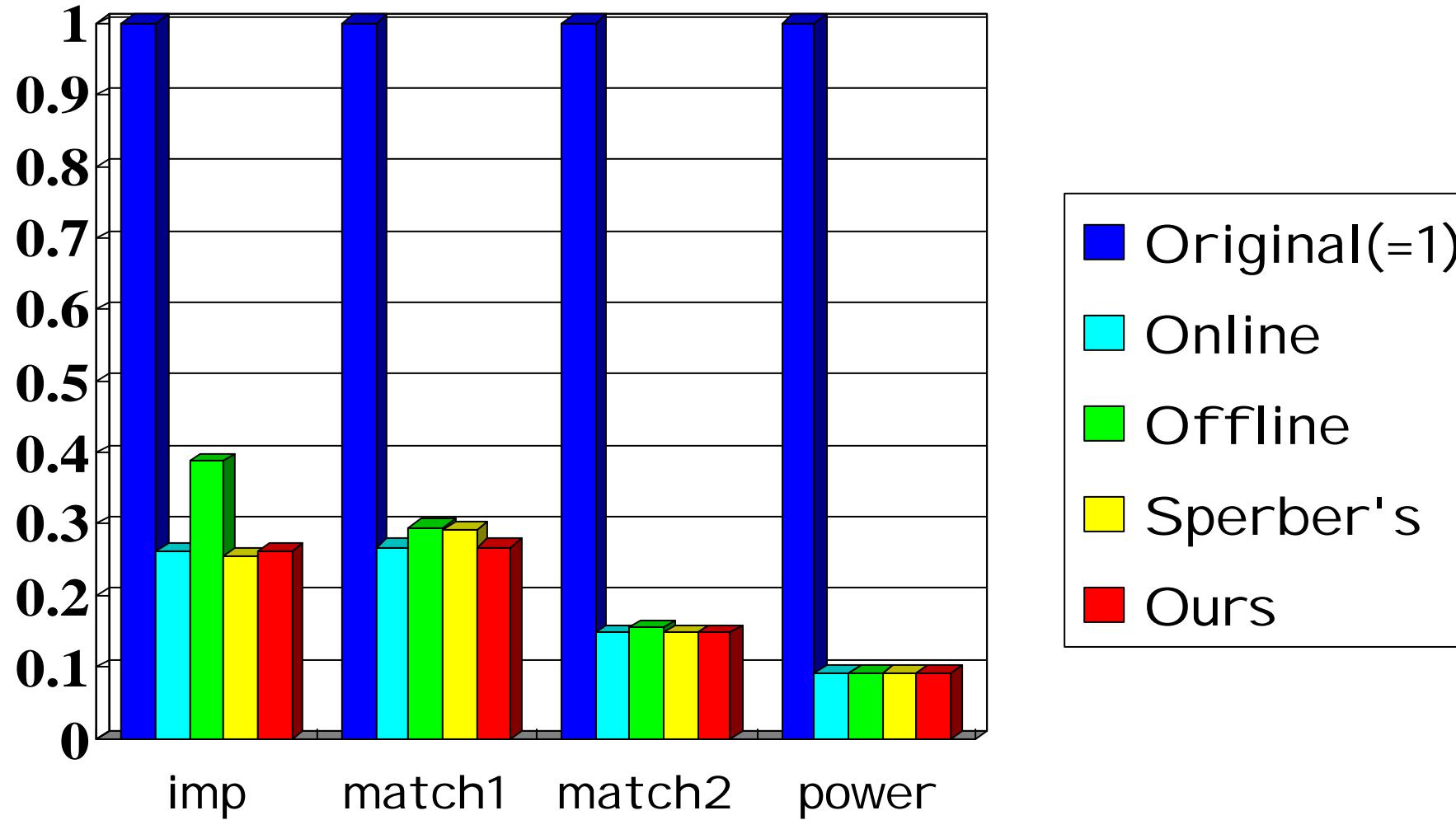
Environment

- Mobile Pentium II 400MHz
- 128MB Main Memory
- Linux 2.2.10
- SML/NJ 110.0.3

Time for Specialization



Time for Specialized Programs



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Related Work (I)

- [Sperber-96]
BTA with "unknown" (T, w)
- [Asai-99]
BTA with "both" (w, w)
- [Bondorf-90]
"Abstract occurrence counting analysis" to decrease unnecessary let-insertions

Our analysis subsumes all of these.

Related Work (II)

- [Ruf-93] [Sperber-96]
(Quasi-)self-application for online PE
- [Thiemann-99]
Systematic derivation of a cogen
approach to offline PE

*We adopted the cogen approach
(which is simpler and faster)
into online-and-offline PE.*

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Conclusion

- We presented "hybrid" PE combining:
 - the precision of online PE, and
 - the efficiency of offline PE
- Future work includes:
 - correctness proof
 - experiments with larger programs