## Foundations of Software Science (ソフトウェア基礎科学) / Foundations of Computer Software (ソフトウェア基礎)

## Homework

## October 16, 2009

## Eijiro Sumii (Instructor)

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Submit on or before October 22, 2009 (next Thursday) by e-mail to:

sumii@ecei.tohoku.ac.jp

The subject line of the e-mail must be

software homework 2

all in lower case and ascii (半角) characters.

Write your student id (including all alphabets and digits) and full name in the first line of the message body of the e-mail.

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- 1. Which of the following  $\lambda$ -terms are grammatically correct?
  - (a) x
  - (b)  $\lambda x$
  - (c)  $\lambda x.y$
  - (d)  $\lambda x.xx$
  - (e)  $\lambda x. \lambda y.x$
  - (f)  $\lambda x.x \lambda y$
  - (g)  $\lambda x.x(\lambda y.z)$
- 2. Show every step of the reduction of the following  $\lambda$ -terms.
  - (h)  $(\lambda a.a)(\lambda b.b)(\lambda c.c)(\lambda d.d)$
  - (i)  $(\lambda x.xx)(\lambda y.y)$
  - (j)  $(\lambda a. \lambda b.b)xy$
  - (k)  $(\lambda x.xx)(\lambda y.yy)$